

# Logarithmic Properties:

$(b > 0 \text{ and } b \neq 1)$

$$f(x) = b^x \quad \Leftrightarrow \quad f^{-1}(x) = \log_b X$$

$$b^E = N \Leftrightarrow \log_b N = E$$

$$e^E = N \Leftrightarrow \ln N = E$$

$$\log_b b = 1$$

$$\ln e = 1$$

$$\log_b X^n = n \log_b X$$

$$\log_b a = \frac{1}{\log_a b}$$

$$b^{\log_b N} = N$$

$$\log_b \frac{1}{a} = -\log_b a$$

$$\log_b X + \log_b Y = \log_b XY$$

$$\log_b X - \log_b Y = \log_b \frac{X}{Y}$$

$$\log_b a = \frac{\log(a)}{\log(b)} = \frac{\ln(a)}{\ln(b)}$$

$$\log_{a^m}(a^n) = \frac{n}{m}, \quad m \neq 0$$

$$\log_{\left(\frac{1}{a}\right)} b = -\log_a b$$

$$\log_a b \cdot \log_b c = \log_a c$$