

Algebra Formula Sheet

Quadratic Function	Factoring	Absolute Value		
$f(x) = ax^2 + bx + c = a(x - h)^2 + h$ $\Delta = \text{discriminat} = b^2 - 4ac$ Vertex of a Parabola : (h, k) $(h, k) = \left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right) = \left(-\frac{b}{2a}, \frac{-\Delta}{4a}\right)$	$(a^2 - b^2) = (a - b)(a + b)$ $(a^4 - b^4) = (a - b)(a + b)(a^2 + b^2)$ $(a^3 + b^3) = (a + b)(a^2 - ab + b^2)$ $(a^3 - b^3) = (a - b)(a^2 + ab + b^2)$	$ x = \begin{cases} x & x \geq 0 \\ -x & x < 0 \end{cases}$ $n^{\text{th}} \text{ root of } x^n$ $\sqrt[n]{x^n} = \begin{cases} x & \text{if } n \text{ is even} \\ x & \text{if } n \text{ is odd} \end{cases}$		
Quadratic Formula	Slope (m)	Midpoint & Distance		
If $ax^2 + bx + c = 0, a \neq 0,$ $\Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-b \pm \sqrt{\Delta}}{2a}$	$P_1(x_1, y_1) \& P_2(x_2, y_2)$ $m = \frac{\text{Rise}}{\text{Run}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$	$M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$ $d(P_1, P_2) = \sqrt{(\Delta x)^2 + (\Delta y)^2}$		
Arithmetic Series	Geometric Series			
$f(1) = a_1$ $a_n = a_1 + (n - 1)d$ $f(n) = f(n - 1) + d, \quad n \geq 2$ $S_n = \frac{n}{2}(a_1 + a_n) = \frac{n}{2}[2a_1 + (n - 1)d]$	$a_n = a_1 r^{n-1}$ $f(1) = a_1$ $f(n) = r \cdot f(n - 1), \quad n \geq 2$ $S_n = \frac{a_1(1 - r^n)}{1 - r}, \quad S_\infty = \frac{a_1}{1 - r} \text{ where } r < 1$			
Complex Numbers	Inverse Function	Permutation & Combination		
$a + ib$ is a complex number Where $i = \sqrt{-1} \Rightarrow i^2 = -1$ $\sqrt{-b} = i\sqrt{b}$ for $b > 0$	$(f \circ f^{-1})(x) = f(f^{-1}(x)) = x$ $(f^{-1} \circ f)(x) = f^{-1}(f(x)) = x$	${}^n P_r = \frac{n!}{(n - r)!}$ ${}^n C_r = \binom{n}{r} = \frac{n!}{(n - r)! r!}$		
	Factorial			
	$n! = n \cdot (n - 1) \cdot \dots \cdot 3 \cdot 2 \cdot 1$			
Pascal Triangle	Binomial Theorem			
$\begin{matrix} \binom{0}{0} & & & & & & \\ \binom{1}{0} \binom{1}{1} & & & & & & \\ \binom{2}{0} \binom{2}{1} \binom{2}{2} & & & & & & \\ \binom{3}{0} \binom{3}{1} \binom{3}{2} \binom{3}{3} & & & & & & \\ \binom{4}{0} \binom{4}{1} \binom{4}{2} \binom{4}{3} \binom{4}{4} & & & & & & \end{matrix}$	1 $1 \ 1$ $1 \ 2 \ 1$ $1 \ 3 \ 3 \ 1$ $1 \ 4 \ 6 \ 4 \ 1$	$(a + b)^n = \binom{n}{0} a^n + \binom{n}{1} a^{n-1} b + \dots + \binom{n}{r} a^{n-r} b^r + \dots + \binom{n}{n} b^n$ $\text{where } \binom{n}{r} = \frac{n!}{(n - r)! r!} \quad \& \quad \binom{n}{r - 1} + \binom{n}{r} = \binom{n + 1}{r}$ $r^{\text{th}} \text{ term of a binomial expansion} = \binom{n}{r - 1} a^{n - r + 1} b^{r - 1}$		
E.g. $(a + b)^4 = \binom{4}{0} a^4 b^0 + \binom{4}{1} a^3 b^1 + \binom{4}{2} a^2 b^2 + \binom{4}{3} a^1 b^3 + \binom{4}{4} a^0 b^4 = a^4 + 4a^3 b + 6a^2 b^2 + 4ab^3 + b^4$				
Exponential Properties ($a \neq 0, b \neq 0$)	Forms for the Equation of a line			
$b^0 = 1$ $b^m b^n = b^{m+n}$	$y = mx + b$	Slope intercept form: m & $P(0, b)$		
$\frac{b^m}{b^n} = b^{m-n}$ $(b^m)^n = b^{mn}$	$y - y_1 = m(x - x_1)$	Point slope form: $P(x_1, y_1)$ & m		
$b^{-n} = \frac{1}{b^n}$ $(ab)^n = a^n b^n$	$\frac{x}{a} + \frac{y}{b} = 1$	Intercept form: $P_1(a, 0)$ & $P_2(0, b)$		
$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$ $\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n$	$Ax + By = C$	Standard form: A, B & C are integers		
$\frac{1}{b^n} = \sqrt[n]{b}$ $\frac{b^m}{b^n} = \sqrt[n]{b^m} = (\sqrt[n]{b})^m$	$x = a$ $y = b$	Vertical line: Contains $P(a, 0)$ Horizontal line: Contains $P(0, b)$		
Logarithm Properties ($b \neq 0, b \neq 1$)				
$b^E = N \Leftrightarrow \log_b N = E$ $e^E = N \Leftrightarrow E = \ln N$	$\log_b x + \log_b y = \log_b xy$	$\log_b x - \log_b y = \log_b \left(\frac{x}{y}\right)$		
$\log_b b = 1$	$\log_b x^n = n \log_b x$	$b^{\log_b N} = N$	$\log_b a = \frac{\log(a)}{\log(b)}$	$\ln(a) = \frac{1}{\log_a e}$
$\ln e = 1$				
$\log_b a = \frac{1}{\log_a b}$	$\log_b \frac{1}{a} = -\log_b a$	$\log\left(\frac{1}{a}\right) b = -\log_a b$	$\log_a b \cdot \log_b c = \log_a c$	$\log_a^m (a^n) = \frac{n}{m}$